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# **PHYS 4520: Physics in Meteorology**

**Introduction to the Earth's atmosphere**

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# Atmospheric science: weather forecast

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- atmospheric models

*based on physical principles from fluid dynamics, thermodynamics,...etc*

- parameterization

*represents phenomena at the unresolved scales of the model*

- observational systems

*acquire various weather variables (e.g. temperature, pressure) using radar, satellite, GPS*

- data assimilation:

*combines information from current data (based on imperfect observation) and from a short-term forecast (based on a model) to produce a current state estimate.*

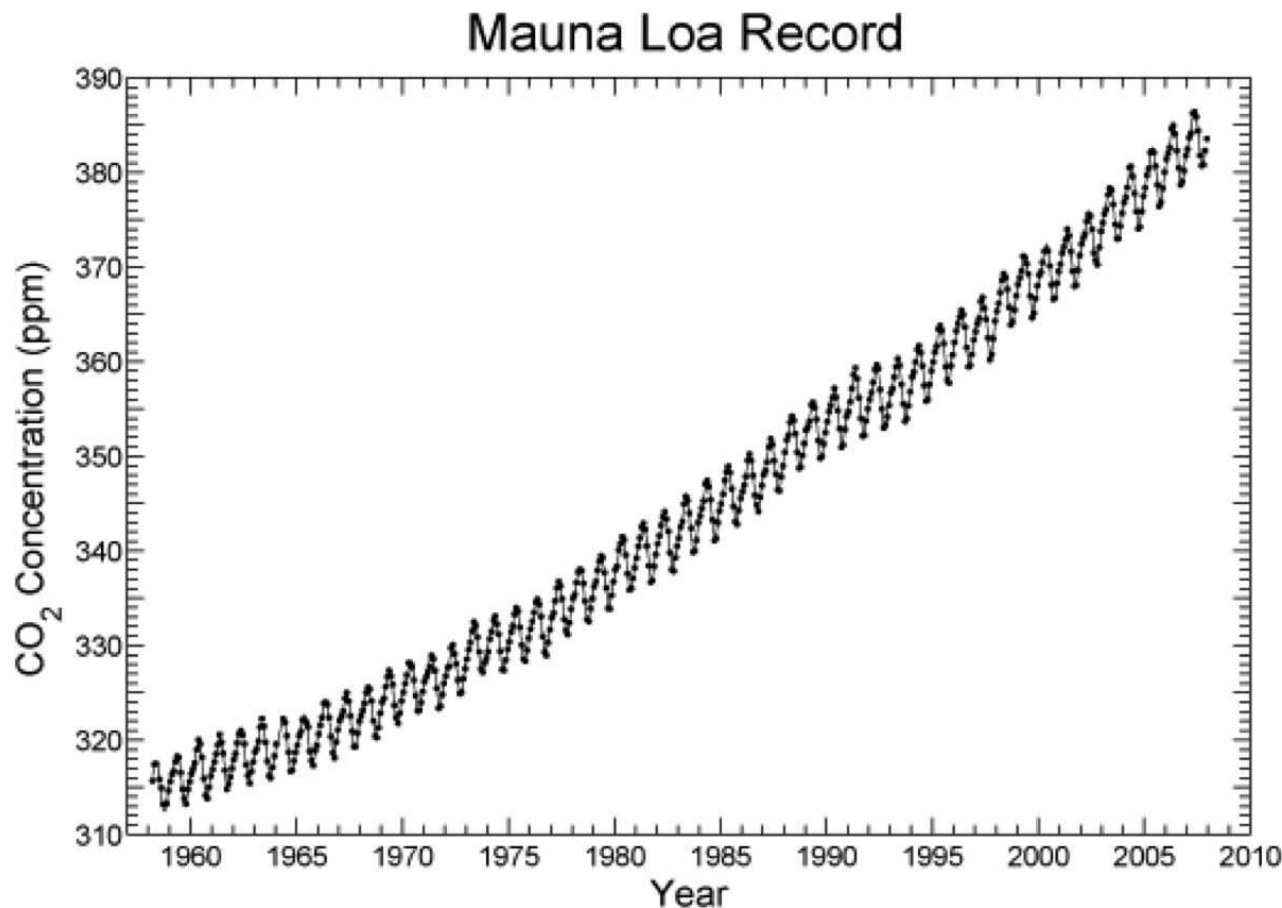
# Atmospheric science: atmospheric chemistry

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- Ozone depletion
  - ozone absorbs UV radiation from the Sun
  - 1974: Crutzen, Rowland and Molina proposed CFCs may reduce ozone concentration in the atmosphere
  - CFC dissociated by UV light releasing Cl atom which is a catalyst of the destruction of ozone
  - 1985: Antarctic ozone hole discovered by Farman, Gardiner and Shanklin
  - Montreal Protocol
    - 1987: specified a 50% reduction in CFCs production
    - 1990: complete phase out of CFCs by early 21st century
  - 1995: Crutzen, Molina, and Rowland were awarded the Nobel Prize in Chemistry

# Atmospheric science: climate dynamics

- Greenhouse warming
  - human-induced warming due to the buildup of greenhouse gases (e.g. CO<sub>2</sub>) in the atmosphere
  - Keeling curve (*Scripps Institution of Oceanography*, <http://scrippsco2.ucsd.edu>)

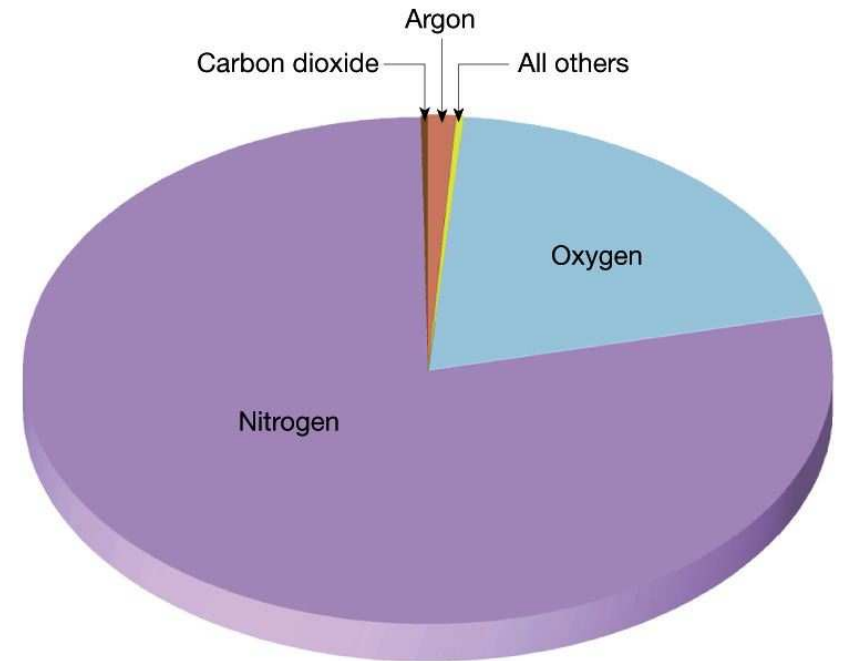


# Composition of the atmosphere

Constituent	Fractional concentration by volume
Nitrogen (N <sub>2</sub> )	78.08%
Oxygen (O <sub>2</sub> )	20.95%
Argon (Ar)	0.93%
Water vapor (H <sub>2</sub> O)	0 – 5%
Carbon dioxide (CO <sub>2</sub> )	380 ppm
Neon (Ne)	18 ppm
Helium (He)	5 ppm
Methane (CH <sub>4</sub> )	1.75 ppm
Krypton (Kr)	1 ppm
Hydrogen (H <sub>2</sub> )	0.5 ppm
Nitrous oxide (N <sub>2</sub> O)	0.3 ppm
Ozone (O <sub>3</sub> )	0 – 0.1 ppm

ppm: parts per million = 0.0001%

(Atmospheric Science, Wallace & Hobbs)



(The Atmosphere, Lutgens & Tarbuck)

# Composition of the atmosphere

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- **Nitrogen and Oxygen** (~ 99%)  
*of little or no importance in affecting weather phenomena*
- **Water vapor** (highly variable, up to 5%)  
*significantly affects our weather and climate: cloud, fog, thunderstorm, tropical cyclone, tornado, hail*
- **Carbon dioxide** (~ 0.038%)  
*significantly affects our climate through the greenhouse effect*
- **Ozone** (~ 0.0000005%, layered 25km from surface)  
*protect living things on Earth from ultraviolet radiation from the Sun*

# Vertical structure of the atmosphere

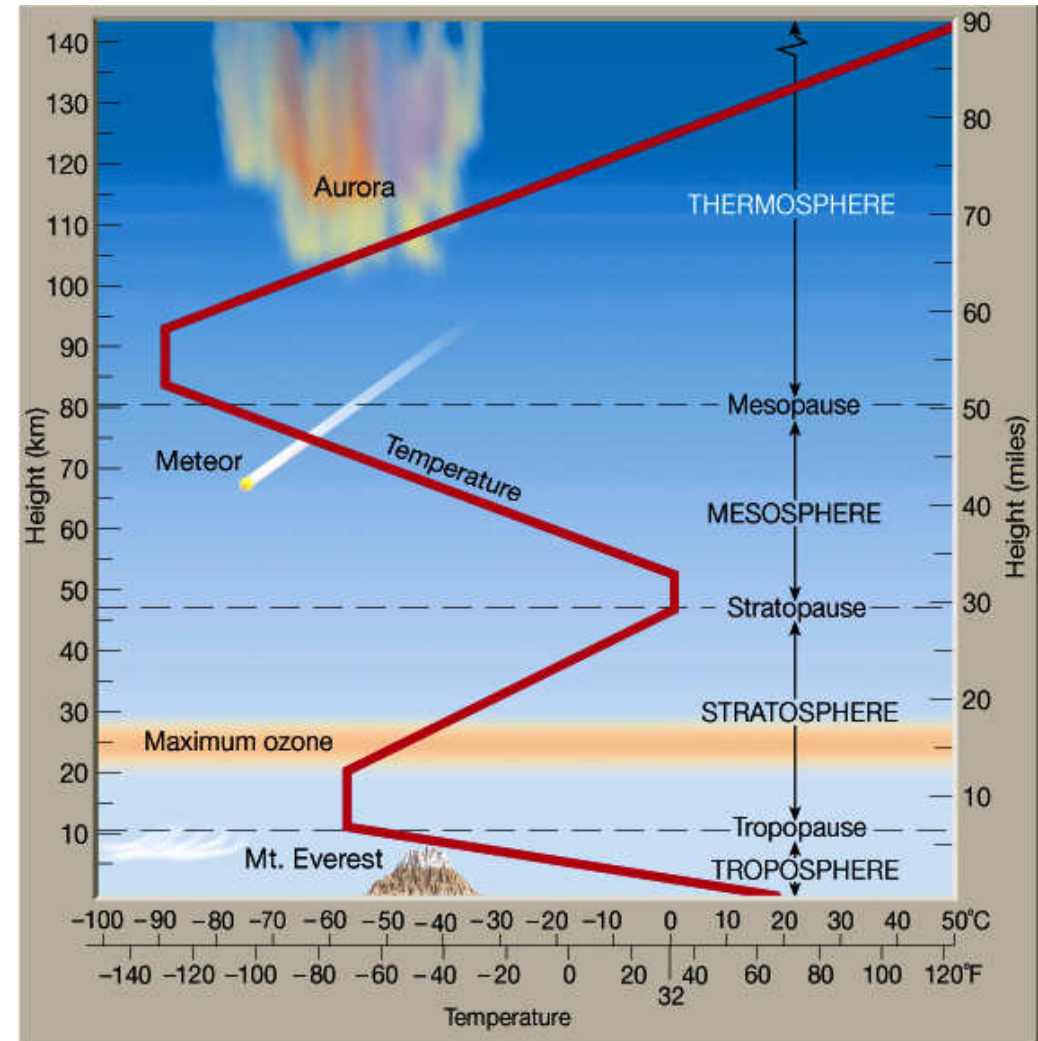
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- a **thin** layer of gas surrounding the Earth  
"thickness" of the atmosphere,  $h \sim 50$  km  
radius of the Earth,  $R \approx 6400$  km  
 $h \ll R \Rightarrow$  **thin**
- variation with height  $z$  of thermodynamic properties: **temperature** ( $T$ ), **pressure** ( $p$ ) and **density** ( $\rho$ )

# Vertical profile of atmospheric temperature

## Troposphere and Tropopause (0 – 20 km)

- contained about 80% of the mass of the atmosphere
- heated from below by the Earth's surface
- **lapse rate**  $\Gamma \equiv \frac{\partial T}{\partial z} \approx -7^\circ\text{C}/\text{km}$
- temperature inversion: embedded layer with  $\Gamma > 0$
- contains nearly all the atmospheric water vapor, the moving weather systems and the associated clouds are almost entirely confined to this layer
- large-scale turbulence and **mixing**

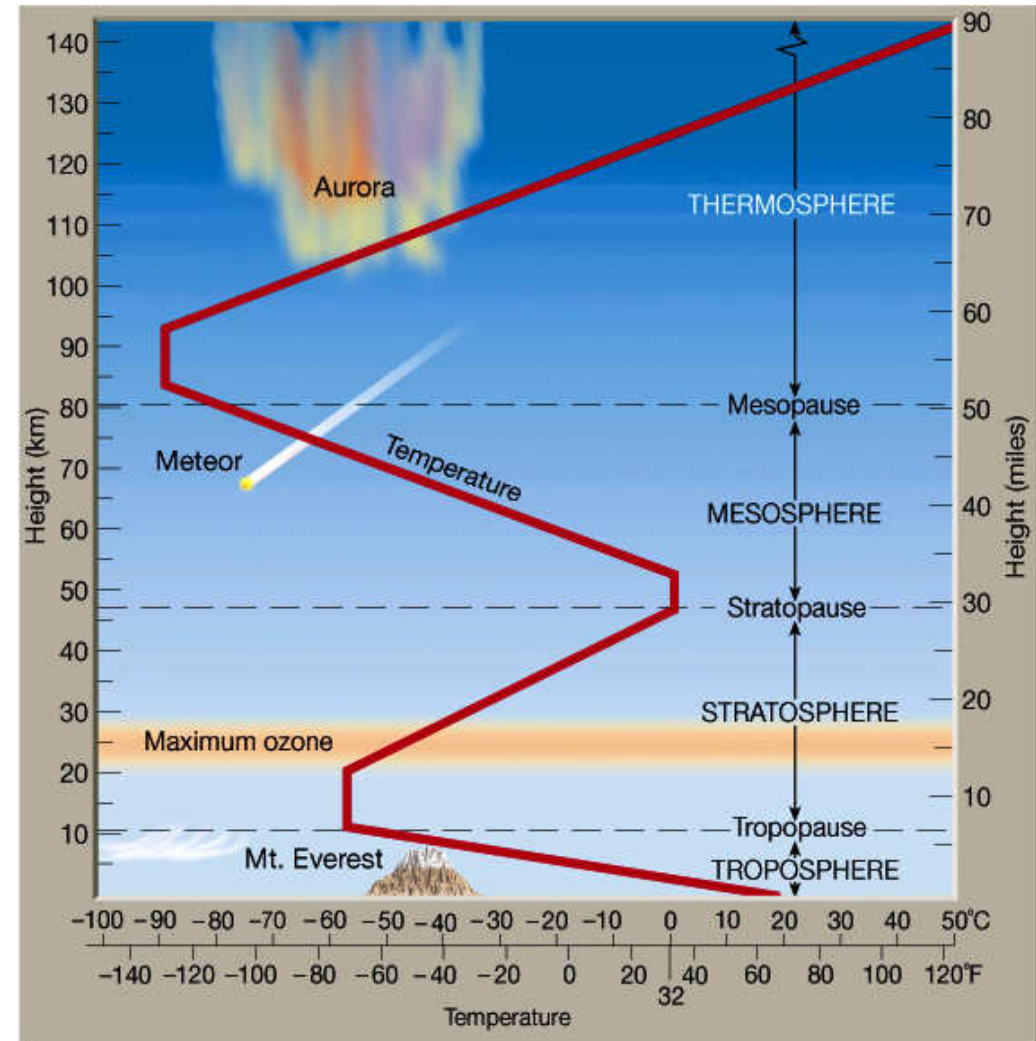




# Vertical profile of atmospheric temperature

## Stratosphere and Stratopause (20 – 50 km)

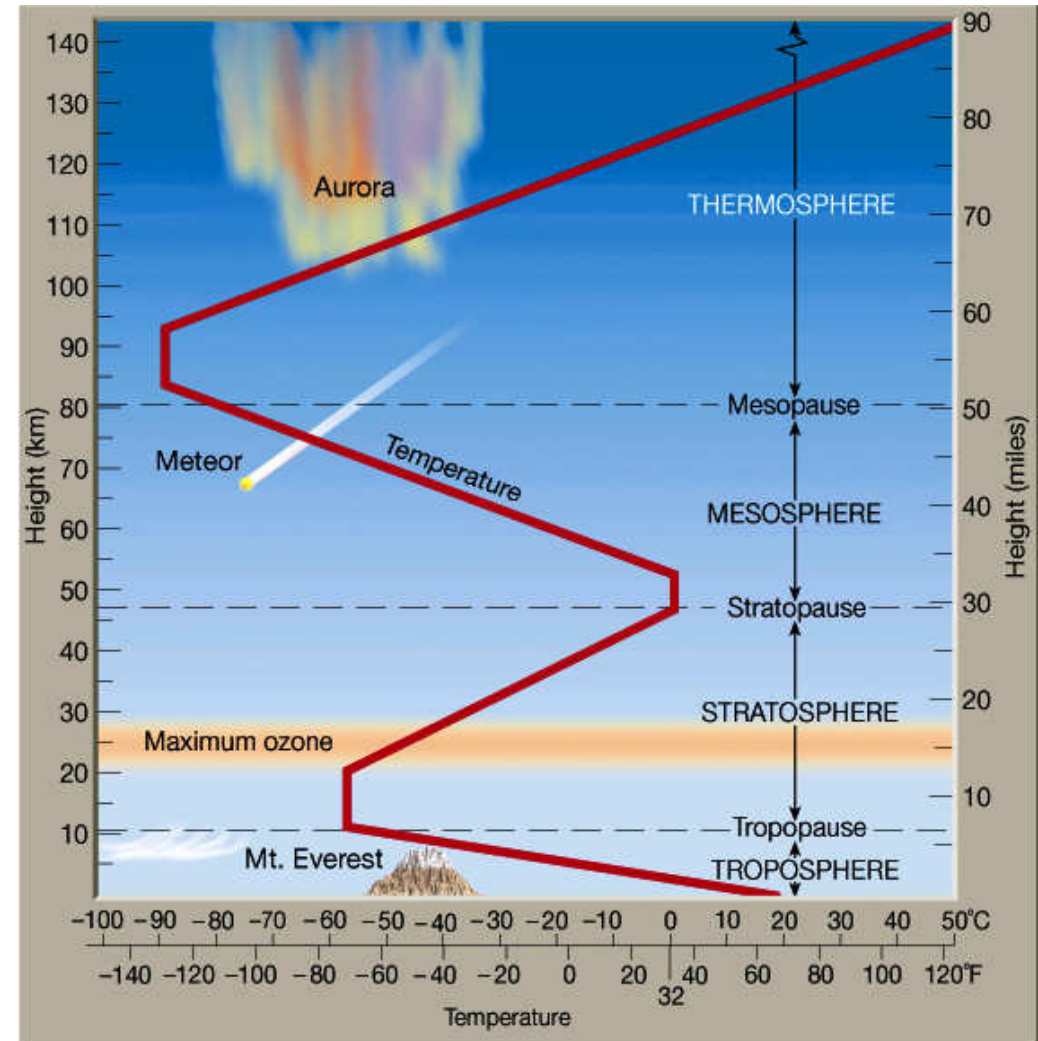
- temperature increases slowly with height up to about 30 km, above which it rises rapidly
- free from cloud and weather phenomena, vertical mixing is inhibited by the stratification of temperature
- **ozone layer** formed here because there is sufficient UV radiation to break  $O_2$  into O atom and enough  $O_2$  molecules to react with the O atom to form  $O_3$
- ozone absorbs UV radiation and releases heat, less UV radiation reaches the lower stratosphere, hence the lower temperature there



# Vertical profile of atmospheric temperature

## Mesosphere and Mesopause (50 – 80 km)

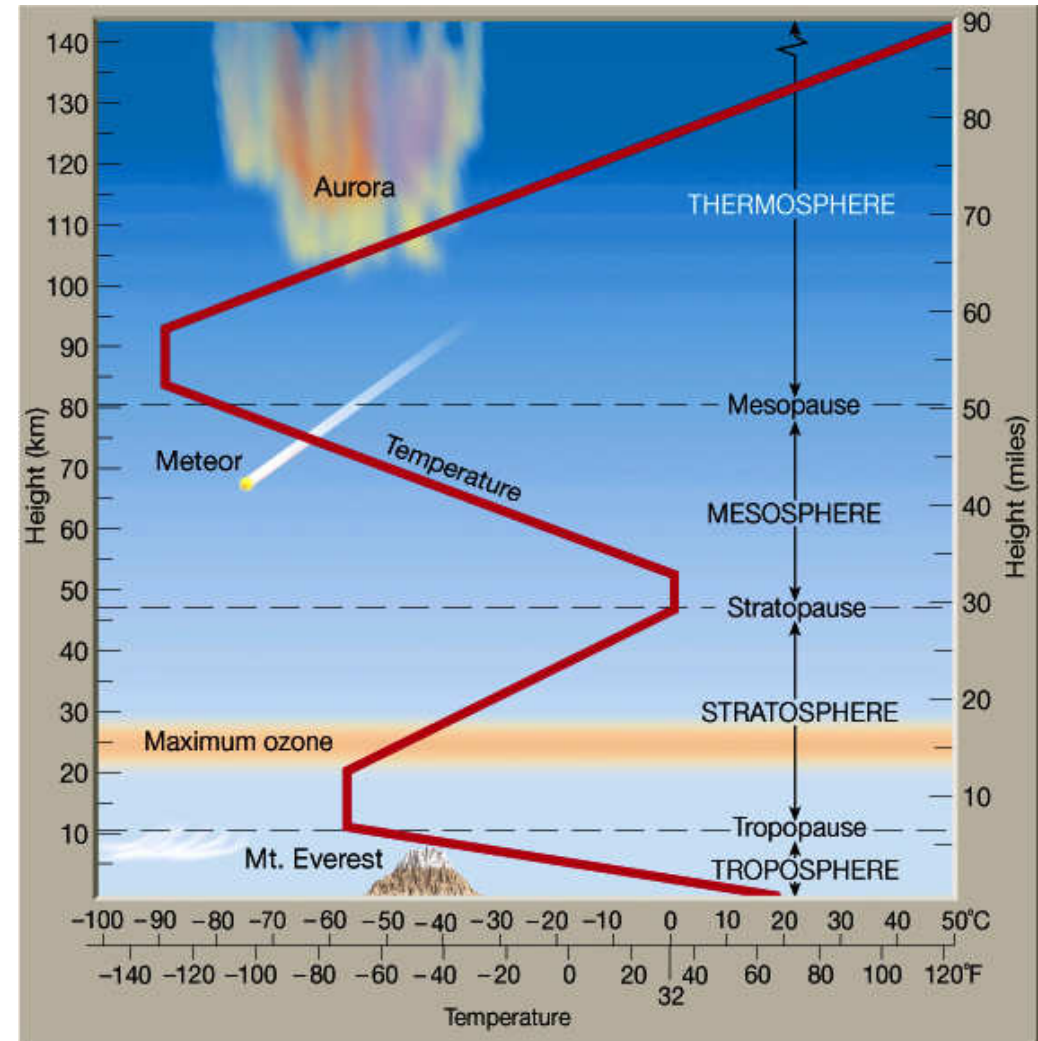
- temperature decreases with height and approaches a **minimum** of about  $-90^{\circ}\text{C}$  at around 80 km
- most meteors enter the atmosphere melt or vaporize here



# Vertical profile of atmospheric temperature

## Thermosphere (80 – 550 km)

- temperature increases with height due to the photodissociation of nitrogen and oxygen molecules and photoionization of their atoms
- temperature in the outer thermosphere varies widely in response to the Sun's activities
- temperature can be over  $1000^{\circ}\text{C}$ , **but...**
- density is extremely low, so one won't feel warm here since there is not enough contact with the few high-speed gas particles to transfer the energy
- Aurora occurs here due the presence of ions

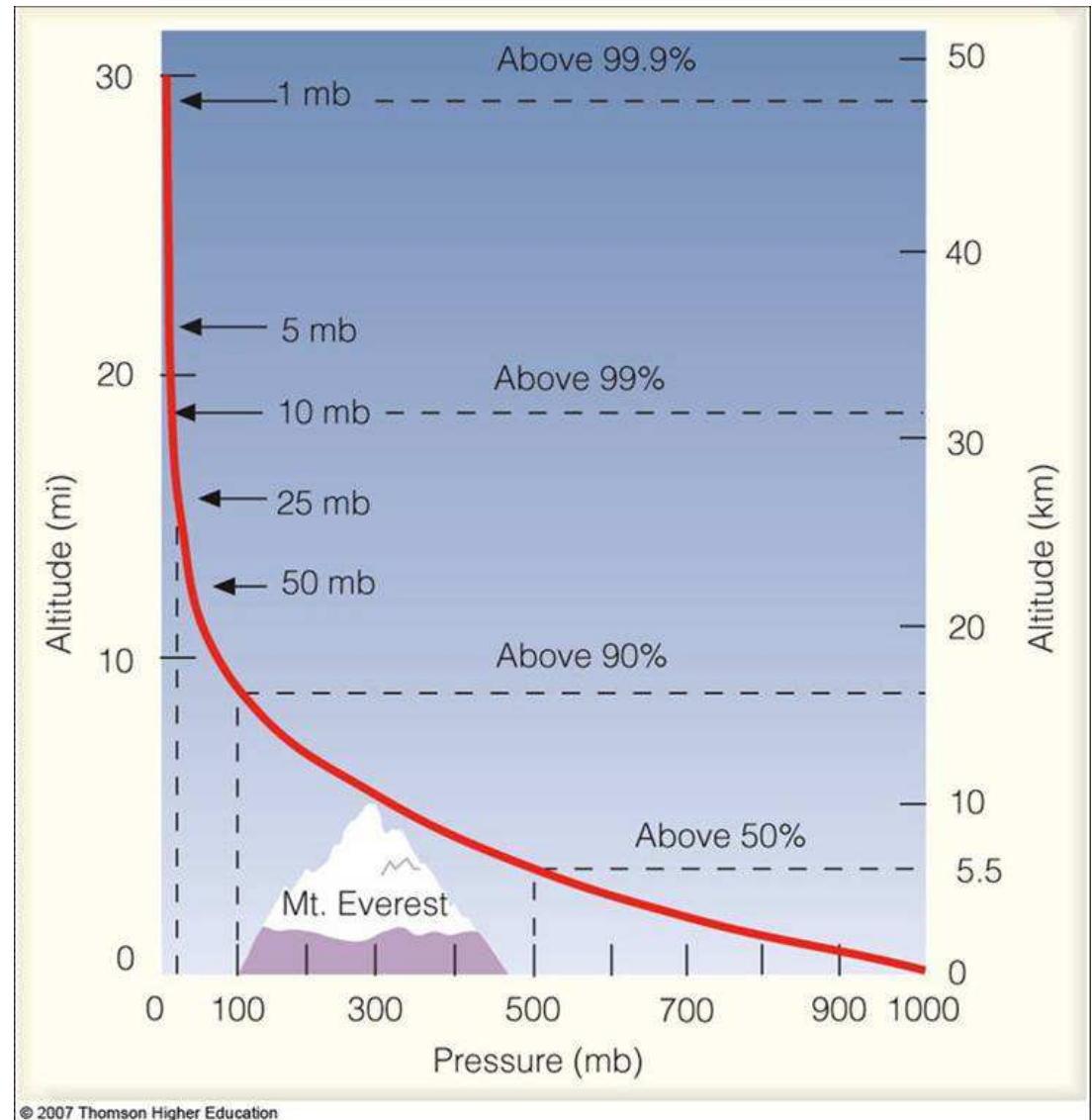


# Vertical profile of atmospheric pressure

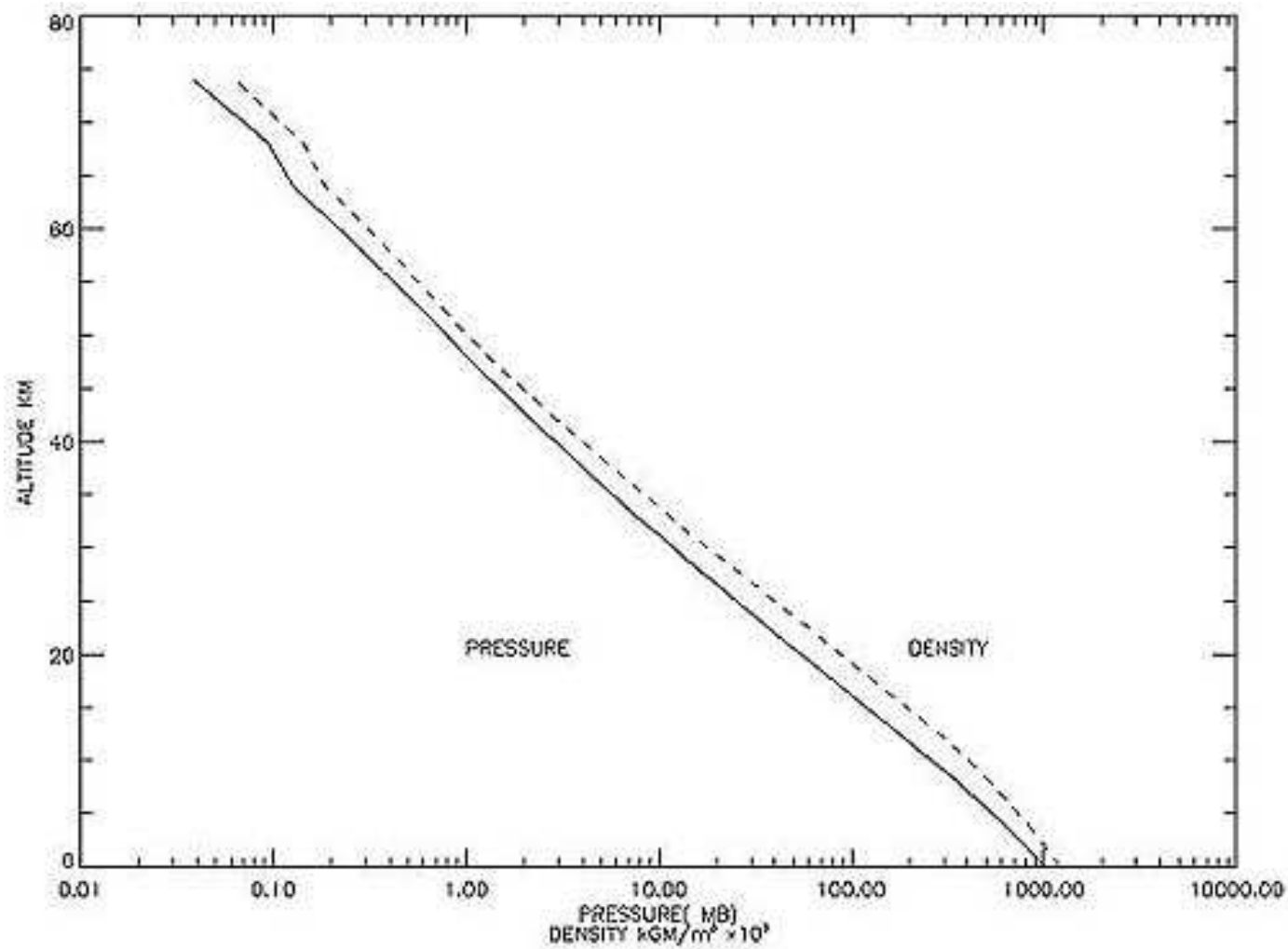
$$p(z) \approx p_0 e^{-z/H}$$

$H$  = scale height

$p_0$  = reference pressure



# Vertical profile of atmospheric density



$$\rho(z) \approx \rho_0 e^{-z/H}$$

# A simple hydrostatic model

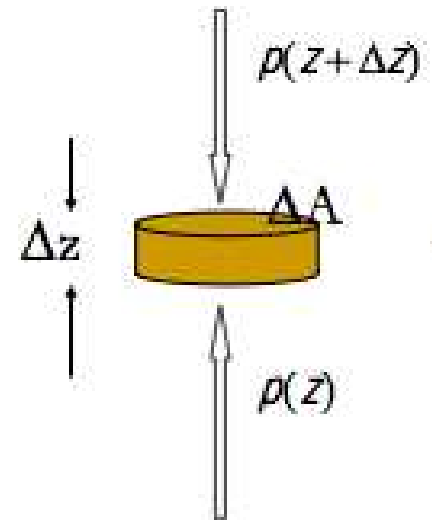
(1) Assume the atmosphere is at rest and in static equilibrium, the net force on a small cylinder of air is zero:

$$p(z) \Delta A = p(z + \Delta z) \Delta A + g \rho(z) \Delta z \Delta A ,$$

$$p(z + \Delta z) \approx p(z) + \Delta z \frac{dp}{dz} .$$

We get the **hydrostatic balance** equation,

$$\frac{dp(z)}{dz} = -\rho(z) g .$$



## A simple hydrostatic model

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(2) Assume the atmosphere behaves as an **ideal gas**:

$$pV = nR^*T,$$

$n$  = number of moles,  $R^*$  = universal gas constant.

In terms of  $\rho$  instead of  $V$ ,

$$p = \rho RT,$$

$R \equiv R^*/M$  where  $M$  is the molar mass.

For dry air,  $M = 0.028964$  kg.



# A simple hydrostatic model

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Combining (1) and (2),

$$\frac{dp}{dz} = -\frac{g}{RT} p,$$

$$p(z) = p_0 \exp \left[ -\frac{g}{R} \int_0^z \frac{1}{T(z')} dz' \right].$$

(3) Assume the atmosphere is **isothermal**:  $T = T_0$ ,

$$p(z) = p_0 e^{-\frac{g}{RT_0} z},$$

$$\rho(z) = \rho_0 e^{-\frac{g}{RT_0} z}.$$

Hence, the scale height  $H = g/RT_0$ .

Take  $T_0 = 290 \text{ K} \Rightarrow H \approx 7.1 \text{ km}$ .