PHYS4520 Physics in Meteorology

Problem Set 7

1. Stream function. If a two-dimensional vector $\vec{u} = (u, v)$ is divergence-free: $\nabla \cdot \vec{u} = 0$, then \vec{u} can be expressed in terms of a scalar stream function $\psi(x, y)$,

$$(u,v) = (-\psi_y,\psi_x).$$

- (a) Verify that \vec{u} given by the above relation is indeed divergence-free.
- (b) For a constant density ideal gas that is in geostrophic and hydrostatic balance on an f-plane,
 - (i) find a stream function for the geostrophic velocity,
 - (ii) find a stream function for the vector (u_z, v_z) [hint: use the thermal wind balance equations].
- 2. "Due to the Coriolis effect, water swirls one way down the toilet in the Northern Hemisphere and the other way in the Southern Hemisphere". Estimate the Rossby number for a toilet and explain whether the above statement is true or not.