**1**. (a) For the GPD, we have:

$$P(X > x) = \lambda_u \left[ 1 + \xi \left( \frac{x - u}{\sigma} \right) \right]_+^{-1/\xi}.$$

Thus, for location A, we have:

$$P(X_A > 32) = 0.009 \left[ 1 + 0.184 \left( \frac{32 - 30}{7.440} \right) \right]^{-1/0.184} = 0.006923.$$

Similarly, for location B we have  $P(X_B > 32) = 0.004051$ . Hence, assuming independence, we have

$$P(X_A, X_B > 32) = 0.006923 \times 0.004051 = 0.00002805.$$

- (b) (i) We must transform the margins to be unit Fréchet-distributed.
  - (ii) We would differentiate G(x, y) with respect to x only (where x represents threshold excesses at location A). We would then substitute the transformed threshold exceedance into this derivative for the rainfall total at location A (i.e.  $\tilde{x}_A$  for x) and the transformed threshold for location B (i.e.  $\tilde{u}_B$  for y).
  - (iii) [There was a typo in the question here should be "32mm = ..." and NOT "50mm = ..."]
    We have

$$P(X_A, X_B > 32) = 1 - \exp\left\{-(986.461^{-1/0.623} + 1605.221^{-1/0.623})^{0.623}\right\} = 0.00128$$

This value is almost 46 times larger than when we assumed independence. This could result in huge under-protection if a flood defence was built to protect against such a combination of extremes at both locations, and rainfall between the locations was assumed independent.

[Total = 9 marks]