

Learning outcomes: Chapter 4

1. You should understand the terms *experiment*, *outcome*, *sample space*, *event*, *independence* and *mutually exclusive*.
2. You should understand the probability scale, and be able to interpret probabilities in plain English.
3. You should be familiar with the *classical*, *frequentist* and *subjective* interpretations of probability, although we will not study *subjective* probabilities in any detail in this course.
4. You should know, and be able to use, the basic laws of probability:
 - The multiplication law (for independent events)
 - The addition law

5. You should be able to construct, and interpret, *tree diagrams*.

6. You should know the conditions that are necessary to assume a *binomial distribution*. You should also:

- Be familiar with the notation used: $X \sim \text{Bin}(n, p)$
- Be able to use the binomial formula for calculating probabilities (assuming independence):

$$P(X = r) = {}^nC_r p^r (1 - p)^{n-r}.$$

- Be able to find the mean and variance for a binomially distributed random variable:

$$E[X] = np, \quad \text{Var}(X) = np(1 - p).$$

7. You should know the conditions that are necessary to assume a *Poisson distribution*. You should also:

- Be familiar with the notation used: $X \sim \text{Po}(\lambda)$
- Be able to use the Poisson formula for calculating probabilities (assuming independence):

$$P(X = r) = \frac{\lambda^r e^{-\lambda}}{r!}.$$

- Be able to find the mean and variance for a Poisson distributed random variable:

$$E[X] = \lambda, \quad \text{Var}(X) = \lambda.$$

8. You should know when you would use a binomial distribution rather than a Poisson distribution, and vice-versa.